Pure 3 May June 2024 Guess Paper CIE A Level Maths 9709



*This is not endorsed by Cambridge and is purely for practice purposes only.

Questions

- 1. Solve the equation $2(3^{2x-1}) = 4^{x+1}$, giving your answer correct to 2 decimal places.[4]
- 2. (a) On an Argand diagram, shade the region whose points represents the complex numbers z satisfying the inequalities $-\frac{1}{3}\pi \leq \arg(z-1-2i) \leq \frac{1}{3}\pi$ and $\Re z \leq 3$. [3]
 - (b) Calculate the least value of $\arg z$ for points in the region from (a). Give your answer in radians correct to 3 decimal places. [2]
- 3. Find, in terms of a, the set of values of x satisfying the inequality

$$2|3x+a| < |2x+3a|,$$

where a is a positive constant. [4]

- 4. (a) Express 5 sin θ + 12 cos θ in the form R cos(θ − α), where R > 0 and 0 < α < ½π. [3]
 (b) Hence solve the equation 5 sin 2x + 12 cos 2x = 6, for 0 ≤ x ≤ π. [4]
- 5. The equation of a curve is $x^3 + 3x^2y y^3 = 3$.
 - (a) Show that $\frac{dy}{dx} = \frac{x^2 + 2xy}{y^2 x^2}$. [4]
 - (b) Find the coordinates of the points on the curve where the tangent is parallel to the x-axis. [5]
- 6. The constant *a* is such that $\int_0^a xe^{-2x} dx = \frac{1}{8}$. (9709/31/M/J/23 number 9)
 - (a) Show that $a = \frac{1}{2} \ln(4a+2)$. [5]
 - (b) Verify by calculation that a lies between 0.5 and 1. [2]
 - (c) Use an iterative formula based on the equation in part (a) to determine a correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]
- 7. Using integration by parts, find the exact value of $\int_0^2 \tan^{-1}\left(\frac{1}{2}x\right) dx$. [5]
- 8. The variables x and y satisfy the differential equation

$$\frac{dy}{dx} = \frac{y^2 + 4}{x(y+4)}$$

for x > 0. It is given that x = 4 when $y = 2\sqrt{3}$.

Solve the differential equation to obtain the value of x when y = 2. [8]

9. Solve the equation

$$\frac{5z}{1+2i} - zz^* + 30 + 10i = 0$$

giving your answers in the form x + iy, where x and y are real. [5]

10. Relative to the origin O, the points A, B and C have position vectors given by

$$\overrightarrow{OA} = \begin{pmatrix} 1\\3\\1 \end{pmatrix}, \quad \overrightarrow{OB} = \begin{pmatrix} 3\\1\\2 \end{pmatrix} \text{ and } \overrightarrow{OC} = \begin{pmatrix} 5\\3\\-2 \end{pmatrix}$$

- (a) Using a scalar product, find the cosine of the angle BAC. [4]
- (b) Hence find the area of triangle ABC. Give your answer in a simplified form. [4]

11. Let
$$f(x) = \frac{21-8x-2x^2}{(1+2x)(3-x)^2}$$
.

- (a) Express f(x) in partial fractions. [5]
- (b) Hence obtain the expansion of f(x) in ascending powers of x, up to and including the term in x^2 . [5]